

Facts and Reminders

Simple Codes

This is a simple code because $43 + 32 = 75$.

$$\begin{array}{r} 43 \\ + 32 \\ \hline AC \end{array} \quad A = 7 \quad C = 5$$

Using Reverse Operations

In the problem below, to crack the code you must subtract 98 from 123. The answer is 25.

Problem	Step	Check	Solution
$\begin{array}{r} 98 \\ + DF \\ \hline 123 \end{array}$	$123 - 98 = 25$	$\begin{array}{r} 98 \\ + 25 \\ \hline 123 \end{array}$	$D = 2 \quad F = 5$

In this next problem, to crack the code, you must divide 1,428 by 42. The answer is 34.

Problem	Step	Check	Solution
$\begin{array}{r} 42 \\ \times AF \\ \hline 168 \\ \underline{1260} \\ 1428 \end{array}$	$1428 \div 42 = 34$	$\begin{array}{r} 42 \\ \times 34 \\ \hline 168 \\ \underline{1260} \\ 1428 \end{array}$	$A = 3 \quad F = 4$

Using Number Sense

In the problem below, you can try two ways to crack the code. One way is to try each digit 1 through 9. Another way is knowing that $6 = 2 \times 3$ and trying 2 first.

Problem	Check	Solution
$\begin{array}{r} 31 \\ \times AA \\ \hline 6A \\ \underline{6A0} \\ 68A \end{array}$	$\begin{array}{r} 31 \\ \times 22 \\ \hline 62 \\ \underline{620} \\ 682 \end{array}$	$A = 2$

In the next problem, you know that the only number that added to itself and equals 2 is 1.

Problem	Check	Solution
$\begin{array}{r} BBB \\ + BBB \\ \hline 222 \end{array}$	$\begin{array}{r} 111 \\ + 111 \\ \hline 222 \end{array}$	$B = 1$

In the problem below, ask yourself the question, "Which number times itself equals 9?" The answer is 3.

Problem	Check	Solution
$\begin{array}{r} FFF \\ \times F \\ \hline 999 \end{array}$	$\begin{array}{r} 333 \\ \times 3 \\ \hline 999 \end{array}$	$F = 3$

Code Cracking

Codes with Addition and Subtraction

Directions: Study the Facts and Reminders page for this unit. Use your knowledge of addition and subtraction to break these codes. Use a calculator if you have one.

$$\begin{array}{r} 1. \quad 54 \\ + 29 \\ \hline \text{JA} \end{array}$$

$$\begin{array}{r} 2. \quad 67 \\ + 99 \\ \hline \text{FII} \end{array}$$

$$\begin{array}{r} 3. \quad 145 \\ + 366 \\ \hline \text{BFF} \end{array}$$

$$\begin{array}{r} 4. \quad 98 \\ + \text{FG} \\ \hline 110 \end{array}$$

$$\begin{array}{r} 5. \quad 87 \\ + \text{CJ} \\ \hline 165 \end{array}$$

$$\begin{array}{r} 6. \quad 247 \\ + \text{ACD} \\ \hline 626 \end{array}$$

$$\begin{array}{r} 7. \quad \text{HF} \\ + 76 \\ \hline 117 \end{array}$$

$$\begin{array}{r} 8. \quad \text{BI} \\ + 99 \\ \hline 155 \end{array}$$

$$\begin{array}{r} 9. \quad \text{DGA} \\ + 756 \\ \hline 1679 \end{array}$$

$$\begin{array}{r} 10. \quad \text{CJ2} \\ + 44\text{B} \\ \hline 1227 \end{array}$$

$$\begin{array}{r} 11. \quad \text{B82} \\ + \text{B11} \\ \hline 1093 \end{array}$$

$$\begin{array}{r} 12. \quad \text{G9E} \\ + 245 \\ \hline 535 \end{array}$$

$$\begin{array}{r} 13. \quad \text{FF} \\ + \text{FF} \\ \hline 22 \end{array}$$

$$\begin{array}{r} 14. \quad \text{AAA} \\ + \text{AA} \\ \hline 366 \end{array}$$

$$\begin{array}{r} 15. \quad \text{HHHH} \\ + \text{HHHH} \\ \hline 8888 \end{array}$$

$$\begin{array}{r} 16. \quad 98 \\ - 38 \\ \hline \text{RM} \end{array}$$

$$\begin{array}{r} 17. \quad 484 \\ - 149 \\ \hline \text{UUN} \end{array}$$

$$\begin{array}{r} 18. \quad 976 \\ - 286 \\ \hline \text{RZM} \end{array}$$

$$\begin{array}{r} 19. \quad 567 \\ - \text{WUX} \\ \hline 333 \end{array}$$

$$\begin{array}{r} 20. \quad 974 \\ - \text{PZO} \\ \hline 176 \end{array}$$

$$\begin{array}{r} 21. \quad 765 \\ - \text{VNV} \\ \hline 614 \end{array}$$

$$\begin{array}{r} 22. \quad \text{QWU} \\ - 134 \\ \hline 689 \end{array}$$

$$\begin{array}{r} 23. \quad \text{PZMV} \\ - 1236 \\ \hline 6665 \end{array}$$

$$\begin{array}{r} 24. \quad \text{ZWUX} \\ - 4265 \\ \hline 4969 \end{array}$$

$$\begin{array}{r} 25. \quad \text{ZZZ} \\ - \text{ZZ} \\ \hline 9\text{MM} \end{array}$$

$$\begin{array}{r} 26. \quad \text{VVVV} \\ - \text{VV} \\ \hline 11\text{MM} \end{array}$$

$$\begin{array}{r} 27. \quad \text{PPZZ} \\ - \text{PP} \\ \hline 7722 \end{array}$$

$$\begin{array}{r} 28. \quad \text{XXXX} \\ - \text{W00W} \\ \hline \text{WX42} \end{array}$$

$$\begin{array}{r} 29. \quad \text{UVV} \\ - 30 \\ \hline 281 \end{array}$$

$$\begin{array}{r} 30. \quad \text{RROR} \\ - \text{UU43} \\ \hline 3263 \end{array}$$

$$\begin{array}{r} 31. \quad \text{WWWWW} \\ - \text{WWW1} \\ \hline \text{w00001} \end{array}$$

$$\begin{array}{r} 32. \quad \text{QQQQQ} \\ - \text{XXX4X} \\ \hline 4\text{XX4X} \end{array}$$

Answer Key

- parallel to EG
23. Line segment GH is parallel to LM
24. Line segment XZ is parallel to VW
25. function of n equals n plus 2
26. function of n equals n times 5
27. function of n equals $(n \text{ times } 4) \text{ plus } 1$
28. function of n equals $(n \text{ divided by } 3) \text{ plus } 2$
29. n is identically equal to 12
30. x is identically equal to x

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- odd numbers
- prime numbers
- even numbers
- letters of the alphabet
- U.S. cities
- tens
- square numbers
- triangular numbers
- shapes
- math signs and symbols
- 11–16. Answers will vary. (Any part of the set is a subset.)

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- 1, 2, 3, 4, 5, 6, 8, 10
- 1, 2, 3, 4, 5, 7, 9, 11
- 1, 3, 4, 6, 9, 10, 15, 16, 21, 25
- 1, 2, 3, 4, 5, 6, 7, 9
- a, b, c, d, e, f, g, i, o, u
- 1, 2, 3, 5, 7, 9, 11, 13
- 2, 4, 6
- 1, 3, 9
- 1
- 1, 3, 5, 7
- a, e
- 3, 5, 7, 11, 13

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- a. 1, 2, 3, 4, 5, 6, 8, 9, 10, 11
- 1, 2, 4, 6

- c. 1, 2
- d. 1, 2
- a. 1, 2, 3, 4, 5, 6, 7, 9, 10, 11, 15, 16, 21, 25
- b. none
- c. 1
- d. none
- a. 2, 3, 4, 6, 8, 9, 10, 12, 14, 15, 16
- b. 6, 12
- c. 4, 8, 12
- d. 12
- a. 4, 6, 8, 12, 16, 18, 20, 24, 28, 30, 32, 36, 40
- b. 24
- c. 8, 16, 24, 32, 40
- d. 24
- Answers will vary.

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- a. 1, 2, 3, 4, 5, 7, 9, 11, 16, 25
- b. 1, 4, 9, 16, 25
- c. 2, 3, 5, 7, 11
- a. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11
- b. 2, 3, 5, 7, 11
- c. 4, 6, 8, 9, 10
- a. a, c, d, e, f, g, h, i, o, u
- b. a, e, i, o, u
- c. c, d, f, g, h
- a. 1, 3, 4, 6, 9, 10, 15, 16, 21, 25, 36
- b. 1, 3, 6, 10, 15, 21
- c. 1, 4, 9, 16, 25, 36
- a. Empty set: J
- b. Universal set: I and J.
- a. Empty set: K
- b. Universal set: K and L.
- 7–8. Answers will vary.

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- 1, 4, 8, 9, 16, 25, 27, 36, 49, 64, 125, 1, 64
- a, b, c, d, e, f, g, h, i, o, u, y
- y

- 12, -10, -8, -6, -4, 2, 4, 6, 8, 10, 12, 14, 16
- none
- $1/2, 1/3, 1/4, 1/5, 1/6, 1/8, 1/9, 1/10, 1/12, 1/15, 1/20, 1/6$
- 2, 3, 4, 5, 6, 7, 8, 9, 10, 12, 6, 12
- 2, 4, 8, 12, 16, 20, 24, 28, 32, 36, 2, 4
- 7–8. Answers will vary.

Page 114

- a. 2, 3, 4, 5, 6, 8, 9, 12, 13, 14, 15, 17, 19, 28
- b. 3, 5, 6, 8, 9, 14, 15, 17, 19, 25, 36
- c. 2, 3, 4, 5, 6, 8, 9, 12, 13, 14, 15, 17, 19, 25, 28, 36
- d. 3, 9
- e. 3, 5, 9
- f. 3, 9
- a. 1, 5, 7, 9, 10, 13, 15, 17, 18, 19, 20, 25, 28
- b. 1, 5, 7, 9, 10, 13, 14, 17, 18, 19, 25, 32
- c. 1, 5, 7, 9, 10, 13, 14, 15, 17, 18, 19, 20, 25, 28, 32
- d. 5, 7
- e. 5, 7, 19
- f. 5, 7
- a. 5, 10, 15, 20, 25, 30, 35, 40, 50, 60, 70, 80, 90, 100, 110
- b. 5, 10, 15, 25, 35, 45, 50, 55, 80, 90, 100, 110
- c. 5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 70, 80, 90, 100, 110
- d. 5, 10, 15
- e. 5, 15, 35
- f. 5, 15

- a. 6, 12, 24, 30, 42, 48, 54, 66, 72, 96
- b. 6, 12, 24, 30, 36, 42, 48, 60, 72, 84, 96, 108
- c. 6, 12, 24, 30, 36, 42, 48, 54, 60, 66, 72, 84, 96, 108
- d. 6, 12, 30
- e. 6, 12
- f. 6, 12

Pages 116–118

Answers will vary.

Pages 120–122

Answers will vary.

Page 124

- J = 8, A = 3
- F = 1, I = 6
- B = 5, F = 1
- F = 1, G = 2
- C = 7, J = 8
- A = 3, C = 7, D = 9
- H = 4, F = 1
- B = 5, I = 6
- D = 9, G = 2, A = 3
- C = 7, J = 8, B = 5
- B = 5
- G = 2, E = 0
- F = 1
- A = 3
- H = 4
- R = 6, M = 0
- U = 3, N = 5
- R = 6, Z = 9, M = 0
- W = 2, U = 3, X = 4
- P = 7, Z = 9, Q = 8
- V = 1, N = 5
- Q = 8, W = 2, U = 3
- P = 7, Z = 9, M = 0, V = 1
- Z = 9, W = 2, U = 3, X = 4
- Z = 9, M = 0
- V = 1, M = 0
- P = 7, Z = 9
- X = 4, W = 2
- U = 3, V = 1
- R = 6, U = 3
- W = 2
- Q = 8, X = 4